

Intercomparison of statistical models for projecting winter oilseed rape yield in Europe under climate change

Behzad Sharif, David Makowski,
Kurt Christian Kersebaum ,
Mirek Trnka , Kirsten Schelde,
Jørgen Eivind Olesen



Outline

- Introduction
- Materials & Methods
- Results
 - Prediction power
 - Inference power
 - Uncertainty
- Conclusions

INTRODUCTION

Some challenges in crop modelling

- Formualted and fitted to the same data
- Based on the past
- The true model is unknown
- Model uncertainties
- Ensemble models
- Pest & disease



Global Change Biology (2014), doi: 10.1111/gcb.12768

Multimodel ensembles of wheat growth: many models are better than one

PIERRE MARTRE^{1,2}, DANIEL WALLACH³, SENTHOLD ASSENG⁴, FRANK EWERT⁵, JAMES W. JONES⁶, REIMUND P. RÖTTER⁶, KENNETH J. BOOTE⁶, ALEX C. RUANE⁷, PETER J. THORBURN⁸, DAVIDE CAMMARANO⁹, JERRY L. HATFIELD⁹, CYNTHIA ROSENZWEIG⁷, PRAMOD K. AGGARWAL¹⁰, CARLOS ANGULO¹⁰, BRUNO BASSO¹¹, PATRICK BERTUZZI¹², CHRISTIAN BIERNATH¹³, NADINE BRISSON^{14,15†}, ANDREW J. CHALLINOR^{16,17}, JORDI DOLTRA¹⁸, SEBASTIAN GAYLER¹⁹, RICHIE GOLDBERG⁷, ROBERT F. GRANT²⁰, LEE HENG²¹, JOSH HOOKER²², LESLIE A. HUNT²³, JOACHIM MINGWERSSEN²⁴, ROBERTO C. IZARRALDE²⁵, KURT CHRISTIAN KERSEBAUM²⁶, CHRISTOPH MÜLLER²⁷, SOORA NAresh KUMAR²⁸, CLAAS NENDEL²⁶, GARRY O'LEARY²⁹, JØRGEN E. OLESEN²⁰, TOM M. OSBORNE³¹, TARU PALOSUO⁶, ECKART PRIESSACK¹³, DOMINIQUE RIPOCHE¹², MIKHAIL A. SEMENOV³², IURII SHCHERBAK¹¹, PASQUALE STEDUTO³³, CLAUDIO O. STOCKLE³⁴, PIERRE STRATONOVITCH³⁵, THILO STRECK²⁴, IWAN SUPIT³⁵, FULU TAO³⁶, MARIA TRAVASSO³⁷, KATHARINA WAHA²⁷, JEFFREY W. WHITE³⁸ and JOOST WOLF³⁹



AARHUS
UNIVERSITY

DEPARTMENT OF AGROECOLOGY



Process Based Models vs. Statistical models in projecting future yields

Process based models	Statistical models
Include several modules	All-in-one
Dynamic	Static
Based on several valuable studies	Empirical and difficult to interpret without prior knowledge
Require calibration	Easier to use
Complicated	Easily understandable
Uncertainty analysis is difficult	Uncertainty analysis can be done easily
Pest & disease correlation with climate variation is often absent	They can indirectly show some "hidden" correlations

Application of statistical methods in yield predictions: Previous studies

- Ordinary Least Squares regression
 - Some studies using quadratic terms/ other regression techniques
- Limited to annual or seasonal averages (of temperature and precipitation)
- No systematic intercomparison of statistical techniques
- Less focus on uncertainty analysis

MATERIALS & METHODS



AARHUS
UNIVERSITY

DEPARTMENT OF AGROECOLOGY

Data

- Climate data
 - Daily temperature, precipitation, radiation
 - Monthly (3*12 parameters) and fortnightly (3*26 parameters) averages over the daily climatic data
- Winter oilseed rape (yield and sowing date)
 - Denmark, Germany, Czech, (France, Belgium)
 - More than 1000 unique (site/year) observations
 - Covering more than 20 years of data up to 2013



Response function

$$\begin{aligned} \text{Yield} = & T_1 * \text{TEMP}_1 + \dots + T_n * \text{TEMP}_n \\ & + P_1 * \text{PREC}_1 + \dots + P_n * \text{PREC}_n \\ & + R_1 * \text{RAD}_1 + \dots + R_n * \text{RAD}_n \\ & + YE * \text{Year} \end{aligned}$$

Monthly resolution: 37 parameters

Forthnightly resolution: 79 parameters

Regression Techniques

- Ordinary Least Squars
- Stepwise regression
- PCR
- PLSR
- Shrinkage methods
 - Ridge
 - Elastic Nets (with alpha values of 0.25, 0.50 and 0.75)
 - Lasso

(R Packages: stats, glmnet, plsr)

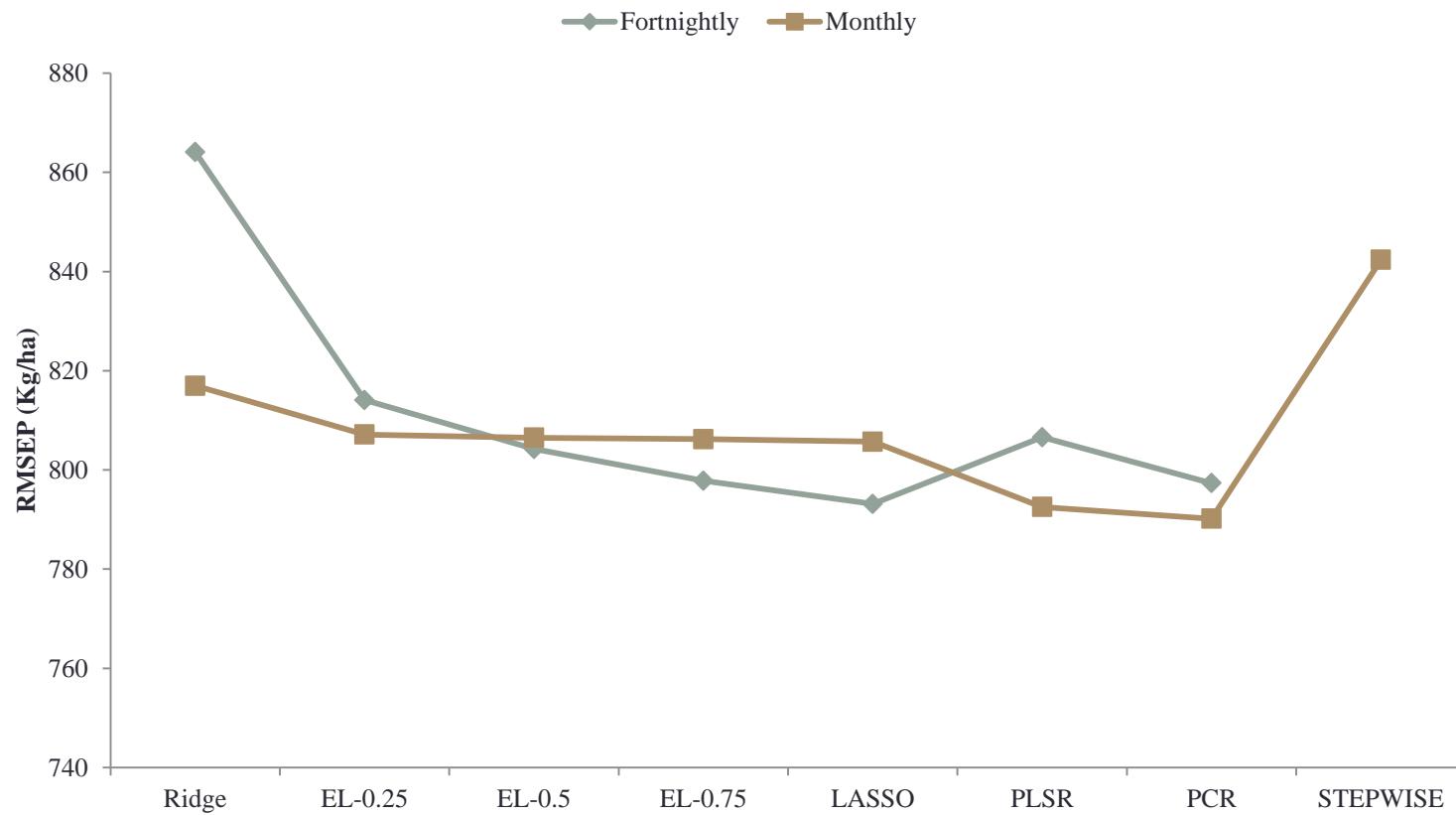
Intercomparison

- Prediction
 - Hold-one-year-out for cross validation
- Inference
 - Features remaining in the final models

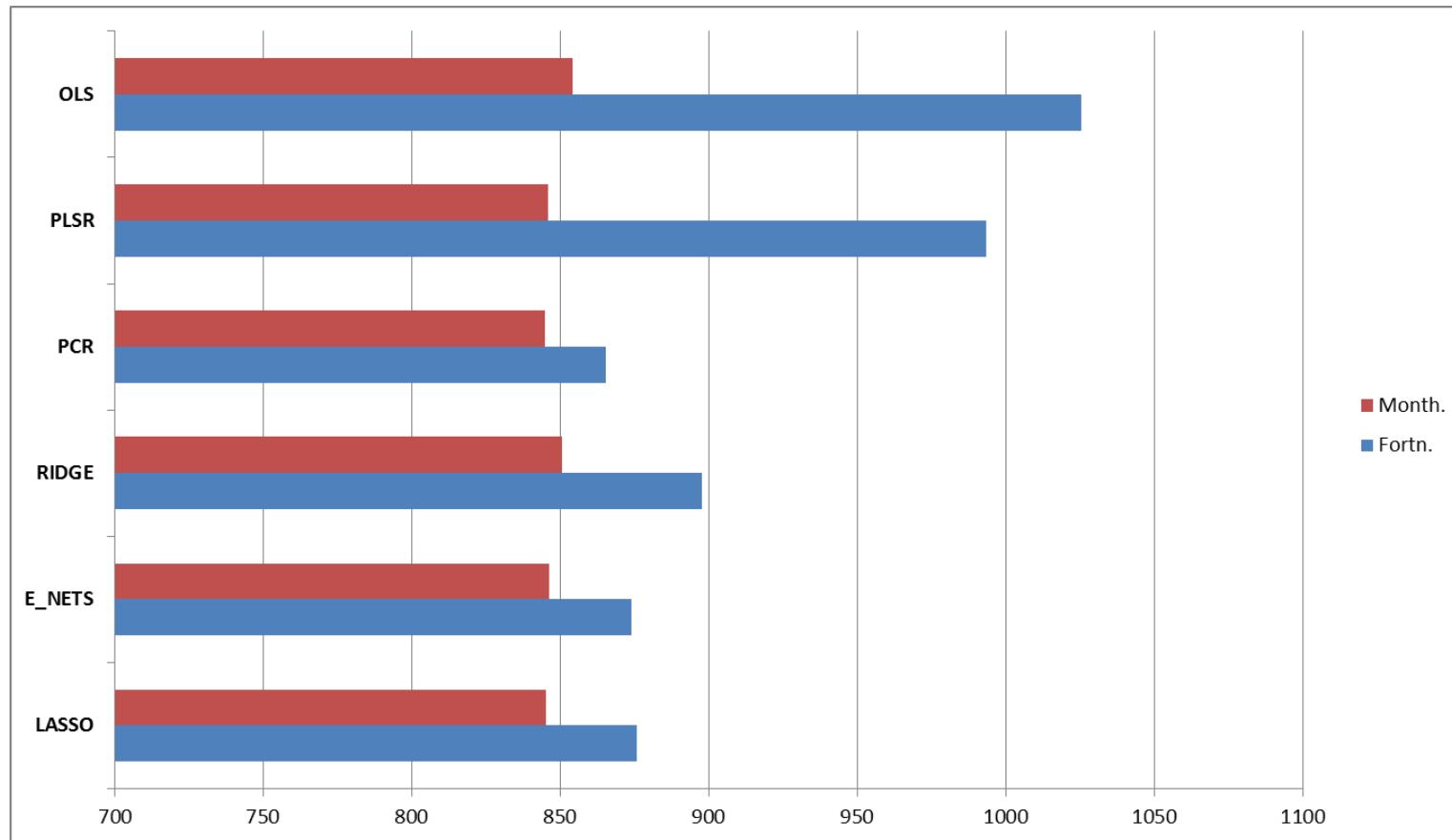
RESULTS

Prediction power

Root Mean Squared Error of Prediction - Denmark



Root Mean Squared Error of Prediction – All countries



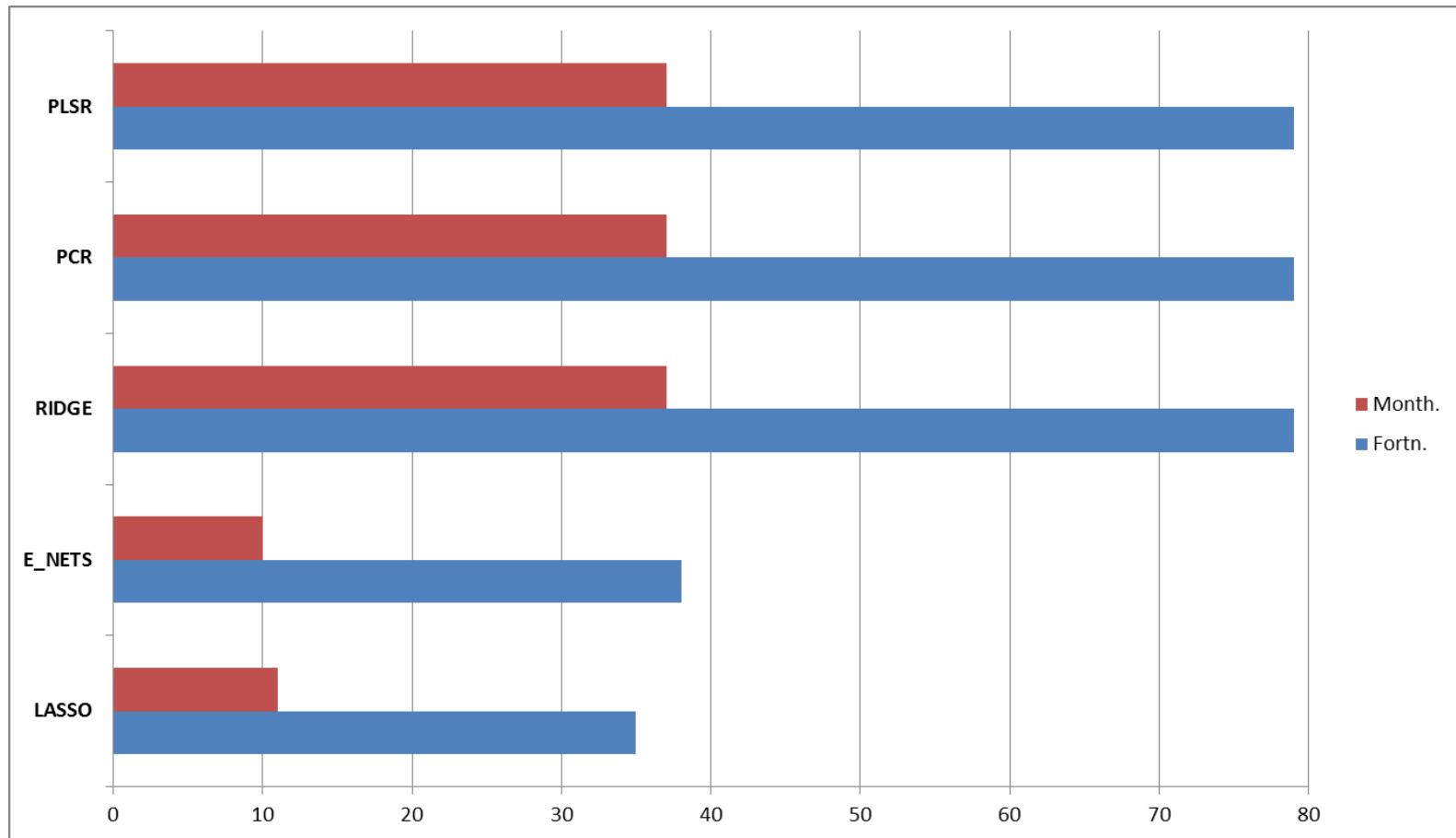
RESULTS

Inference power

Estimated Coefficients - Denmark

Start Date	01-08	15-08	29-08	12-09	26-09	10-10	24-10	07-11	21-11	05-12	19-12	02-01	16-01	30-01	13-02	27-02	12-03	26-03	09-04	23-04	07-05	11-05	04-06	18-06	02-07	16-07	
End Date	14-08	28-08	11-09	25-09	09-10	23-10	06-11	20-11	04-12	18-12	01-01	15-01	29-01	12-02	26-02	11-03	25-03	08-04	22-04	06-05	20-05	03-06	17-06	01-07	15-07	29-07	
Temperature																											
RIDGE	2	6	18	-1	-4	3	-12	25	1	-5	9	2	-10	-7	-3	-8	-3	1	32	24	25	4	-18	-2	2	-2	
ELNET - Alpha =0.25							-23	19			0								44	29	20						
ELNET - Alpha =0.50							-29	9											31	39	13						
ELNET - Alpha =0.75							-32	3											22	48	10						
LASSO							-33												17	53	8						
PLSR	10	10	10	4	-1	-7	-16	12	0	-4	16	8	-13	-9	-3	-13	1	-2	13	11	12	0	-8	0	-7	-4	
PCR	9	10	7	5	1	-11	-15	11	-7	-9	9	9	-20	-6	-6	-18	1	-1	12	4	7	2	0	1	-5	-2	
OLS	9	-18	232	-212	-111	135	13	-68	-36	85	-3	-51	94	24	51	-49	203	-171	12	-150	425	67	-73	208	-87	-263	
STEPWISE		144	-203	-126	101								70				108	-100			354			136		-285	
Radiation																											
RIDGE	4	-17	-7	8	32	24	-27	-70	60	2	-29	-93	13	11	9	14	10	9	16	6	-3	5	-2	-6	-2	-2	
ELNET - Alpha =0.25	3				37			-57											17								
ELNET - Alpha =0.50	6				34			-13											12								
ELNET - Alpha =0.75	9				32														10								
LASSO	11				31														8								
PLSR	16	-5	0	10	10	6	1	-3	0	1	-2	-1	2	-2	0	6	8	2	18	8	4	3	-7	-8	-12	-5	
PCR	16	-3	2	13	8	8	3	-2	0	2	-2	0	4	-1	-4	11	10	-4	16	11	0	7	-3	-6	-12	-1	
OLS	60	98	83	-67	84	-32	-195	-373	73	-216	399	-507	-48	381	-12	-16	-14	-44	132	-15	-129	-108	13	-19	25	113	
STEPWISE	62				162		-397		-496				432						95	-99	-91					82	
Precipitation																											
RIDGE	13	-2	-21	-19	-7	3	-9	-29	8	-9	-19	-1	-6	6	-32	-15	-6	-1	-1	-20	-11	-5	12	1	1	21	
ELNET - Alpha =0.25			-7	-30			-47												-23								
ELNET - Alpha =0.50				-34			-35											-21									
ELNET - Alpha =0.75				-36			-28											-19									
LASSO				-37			-23											-17									
PLSR	2	-2	-7	-12	-3	1	-12	-9	0	-2	-2	2	-3	0	-11	-6	-1	1	-3	-4	-4	-4	2	1	0	5	
PCR	-3	2	-3	-6	-5	2	-7	-5	-2	-2	0	4	-4	0	-9	-6	-2	3	-4	-5	-1	5	3	2	3	4	
OLS	51	-56	-46	-28	2	10	-47	-81	25	59	43	-86	83	57	-190	-75	156	124	8	-277	-32	-2	32	-79	52	138	
STEPWISE	-41	-74					-142											143	-122								

Number of Significant Features in the final model - Czech



RESULTS

Uncertainties

Variance Decomposition – Yield projection under climate change

$$\begin{aligned} V(Y) = & V_M [E_{\varepsilon, \theta}(Y|M)] \\ & + E_M [V_\theta(E_\varepsilon(Y|M, \theta))] \\ & + E_M [E_\theta(V_\varepsilon(Y|M, \theta))] \end{aligned}$$

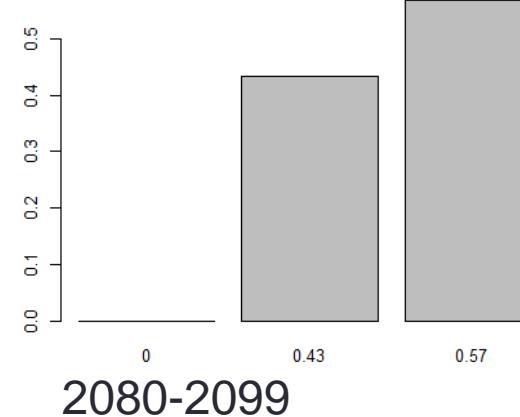
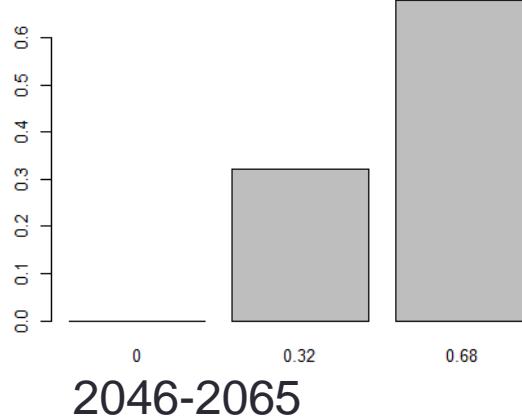
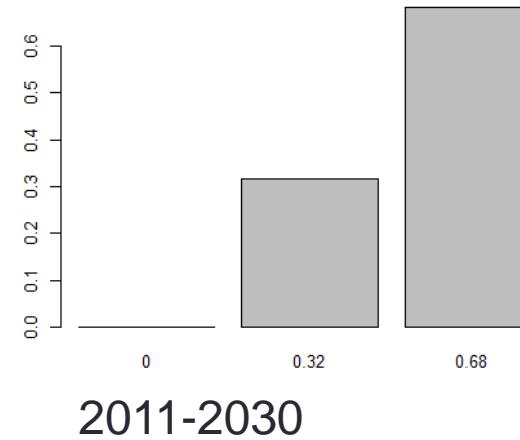
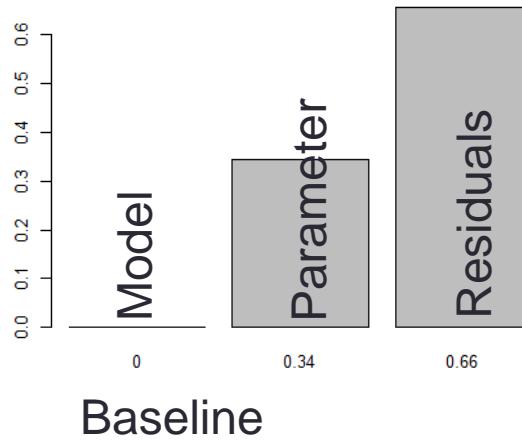
Where

M: Model

θ : Set of parameters

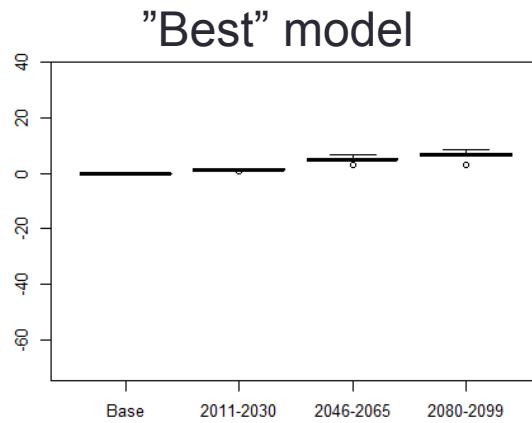
ε : Residual errors

Variance decomposition - Czech

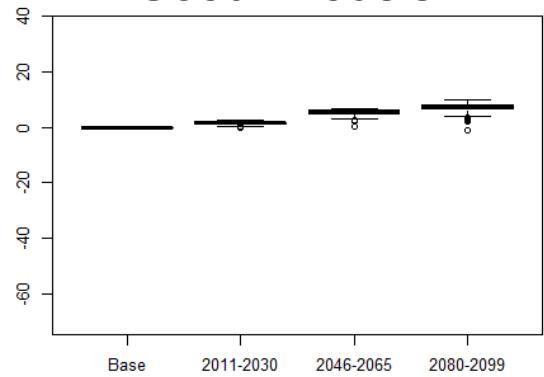


Effect of model and parameter uncertainty percent of yield change predictions - Czech

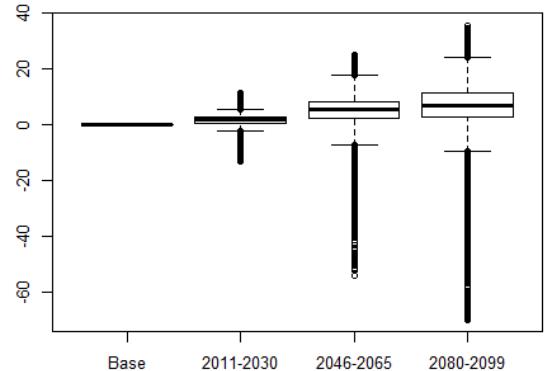
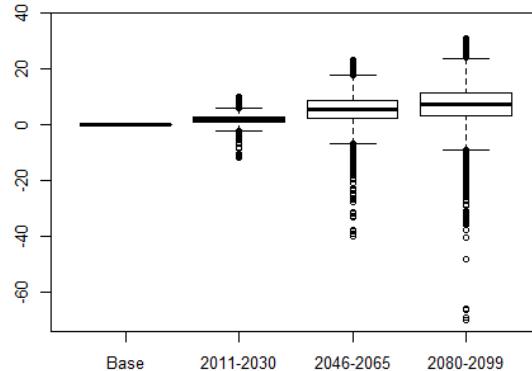
Main Sample



"Good" models



bootstrapping



Conclusions

- State-of-the-art regression techniques could be useful, both in prediction and inference.
- Regression techniques can be useful in pointing out which climatic factors are influential for yield during which growth phases
- Cross-validation of regression models across space (between countries) can provide a method for validating validity for use in climate change projections
- Regression techniques offer a direct method for addressing parameter uncertainty

THANK YOU!
